# **Extracting Transmission (S<sub>21</sub>, S<sub>12</sub>) Parameters of Two-Port Devices Embedded in Nonreflecting Lines**

Determinación de los Parámetros de Transmisión  $(S_{21}, S_{12})$  de Dispositivos de Dos Puertos Montados en Líneas de Transmisión no Reflectoras

J. Apolinar Reynoso Hernández

Centro de Investigación Científica y de Educación Superior de Ensenada (CICESE) División de Física Aplicada, Km. 107 carretera Tijuana-Ensenada, B.C., México CP. 22860 E-mail: apolinar@cicese.mx

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## Abstract

A straightforward broadband method for extracting the  $S_{21}$  and  $S_{12}$ transmission parameters of devices embedded in nonreflecting transmission lines (microstrip or coplanar) is presented. Two nonreflecting transmission lines (L-L method) or a line and a match (L-M method) are used as standards where one line should be twice as long as the lines into which the device is embedded. Two different procedures for de-embedding  $S_{21}$  and  $S_{12}$  are investigated. The first one uses the travelling wave vector  $\lambda$  instead of the wave propagation constant  $\gamma$  of the standard line. The second one, based on a novel matrix approach, uses some parameters of the input transition instead of the wave propagation constant  $\gamma$  or the travelling wave vector  $\lambda$  of standard lines. The performance of this method is shown by the broadband measurement of  $S_{21}$ and  $S_{12}$  of a PHEMT transistor NE24200 (biased at  $V_{ds} = 2 V$ ;  $V_{gs} = 0 V$ ) in the frequency range of 45 MHz-50 GHz and by the determination of the small signal-gain of the commercially available SiGe RFIC model SGA-5386 and SGA-5389 in the frequency range of 45 MHz-10 GHz.

**Key Words:** *de-embedding, Calibration, PHEMTs, Test fixtures, Scattering-parameter, Network Analyzers.* 

#### Resumen

En este artículo se presenta un método de "de-embedding" para determinar los parámetros de transmisión  $S_{21}$  y  $S_{12}$  de cualquier cuadripolo: activo o pasivo. El nuevo método es implementado utilizando dos líneas (coplanares, microcinta, etc) no refelctoras (metodo L-L) y una línea no reflectora y una carga (Metodo L-M). Se presentan dos procediminetos matemáticos para calcular los parámetros S<sub>21</sub> y S<sub>12</sub>. El primer procedimiento se basa en las propiedades de los determinantes y utiliza para efectuar el calculo de  $S_{21}$  y  $S_{12}$  el vector de onda  $\lambda$  en lugar de la constante de propagación y de las líneas en las que el dispositivo se encuentra montado. El sengundo método para calcular  $S_{21}$  y  $S_{12}$ . desarrollado en base a un cálculo matricial original, utiliza el conocimiento parcial de los elementos de la transición TA en lugar del vector de onda  $\lambda$  y la constante de propagación  $\gamma$ . La utilidad del método se demuestra con la medición de los parámetros de transmisión de un transistor PHEMT NE24200 (polarizado a  $V_{ds} = 2 V$ ;  $V_{gs} = 0 V$ ) en el intervalo de frecuencia de 40MHz-50GHz y por la determinación de la ganancia en pequeña señal del amplificador comercial SiGe RFIC modelo SGA-5386 y SGA-5389 en el intervalo de frecuencia de 45 MHz-10 GHz.

**Palabras Clave:** Substracción, Calibración, Transistor Pseudomorfico de Alta Movilidad, Soporte de Pruebas, Medición de Parámetros de Dispersión, Analizador de Redes.

# I Introduction

Non-coaxial devices e.g. chip transistors, chip amplifiers, etc. have to be mounted in a test fixture to be measured. A classical test fixture is formed with two nonreflecting lines (microstrip or coplanar) and two adapters (coaxial connectors or coplanar to microstrip transitions). The test fixture and the Device Under Test (DUT) are shown in Fig. 1. In order to make a full extraction of the DUT scattering parameters S<sub>ij</sub> from the scattering parameters measured at the connectors plane of the test fixture (see Fig. 1), line wave propagation constant  $\gamma$  and adapters S parameters are needed. Calibration techniques such as Line-Reflect-Line LRL (Engen and Hoer, 1979) allow the determination of  $\gamma$ and the adapters S parameters. These error correction techniques use at least three calibration standards. Classical LRL (TRL) is frequency limited by the line electrical length  $\theta$  (20° <  $\theta$  < 160°). This drawback can be overcome if lossy line (Marks R.B, 1991) along with a broadband computation of  $\gamma$  (Reynoso-Hernández J.A, Estrada-Maldonado C. F, 1999) are used.

On the other hand, utilizing the Thru-Line method, Wan(Wan CH, et al 1998) has shown that two line standards are enough for extracting  $S_{21}$  and  $S_{12}$  transmission parameters without the previous knowledge of the adapters' S parameters (Wan CH, et al 1998). However, the use of two lines as reported by (Wan CH, et al 1998), does not allow a broadband de-embedding of transmission parameters. This is because phase discontinuities occurs when  $\gamma$  is computed with [Wan CH, et al 1998, Eq.(4)] or [Lee M.Q et al, Eq.(12)] and then these equations do not operate in a broadband frequency range as suggested by (Reynoso-Hernández J.A, Estrada-Maldonado C. F, 1999). The purpose of this work is to investigate whether two standards are still enough for determining  $S_{21}$  and  $S_{12}$  of the two-port devices mounted in test fixtures with lines of arbitrary length. Moreover, the problem of frequency

restrictions is also considered. Using "long lines" a broadband de-embedding method is presented for transmission  $S_{21}$  and  $S_{12}$  parameters of any two-port device either active or passive, without frequency restrictions and without the previous knowledge of adapters' *S* parameters.

This article is organized as follows: in section II, the L-L method is presented and in section III a straightforward procedure for determining  $S_{21}$  and  $S_{12}$  is presented. Experimental results and discussion are given in section IV. Finally, conclusions are drawn in section V.



Fig. 1. Layout of the calibrations standards (line L1 and line L2) and the test fixture utilized in the method

# 2 Extraction of S<sub>21</sub> AND S<sub>12</sub> Utilizing Two Nonreflecting Lines

The *L-L* (Line-Line) method needs for its implementation two nonreflecting lines and a device embedded in two lines. The line standards used are shown in Fig. 1. The shorter and longer lines will be referred to as  $L_1$ , and  $L_2$ respectively. The two ports referenced as  $T_A$  and  $T_B$ correspond to transitions used for insuring the connection between the lines and the network analyzer at the line input and output ports.  $T_A$  and  $T_B$  include either the microwave probes or coaxial to microstrip microwave connectors (launchers) and the necessary hardware for the network analyzer.

Wave Cascading Matrix, WCM, are used for the modeling of transitions  $T_A$ ,  $T_B$ , line  $L_1$  and line  $L_2$ . The WCM is defined as:  $T_A$  for transition  $T_A$ ,  $T_B$  for transition  $T_B$ ,  $T_{L1}$  for line  $L_1$ , and  $T_{L2}$  for line  $L_2$ . In the following,  $T_A$  and  $T_B$  are assumed to be different. The three WCM  $T_1$ ,  $T_2$ , and  $T_3$  ( $T_1$  for line  $L_1$  plus transitions,  $T_2$  for line  $L_2$  plus transitions,  $T_3$  for device under test embedded in transitions and lines) can be written as

$$\mathbf{T}_{1} = \mathbf{T}_{\mathbf{A}} \ \mathbf{T}_{\mathbf{L}\mathbf{1}} \ \mathbf{T}_{\mathbf{B}} \,, \tag{1}$$

$$\mathbf{T}_2 = \mathbf{T}_{\mathbf{A}} \ \mathbf{T}_{\mathbf{L}2} \ \mathbf{T}_{\mathbf{B}} \,, \tag{2}$$

$$\mathbf{T}_{\mathbf{3}} = \mathbf{T}_{\mathbf{A}} \mathbf{T}_{\mathbf{L}} \mathbf{T}_{\mathbf{DUT}} \mathbf{T}_{\mathbf{L}} \mathbf{T}_{\mathbf{B}} , \qquad (3)$$

where

$$\mathbf{T}_{\mathbf{L}i} = \begin{pmatrix} e^{-\gamma \, Li} & 0 \\ & & \\ 0 & e^{\gamma \, Li} \end{pmatrix} \quad i = 1, 2 , \qquad (4)$$

$$\mathbf{T}_{\mathbf{L}} = \begin{pmatrix} e^{-\gamma \frac{L_1}{2}} & 0 \\ & \frac{\gamma L_1}{2} \\ 0 & e^{\gamma \frac{L_1}{2}} \end{pmatrix},$$
(5)

$$\mathbf{T}_{\mathbf{D}\mathbf{U}\mathbf{T}} = \frac{1}{S_{21}} \begin{pmatrix} -\Delta S & S_{11} \\ -S_{22} & 1 \end{pmatrix},$$
 (6)

$$\mathbf{T}_{\mathbf{A}} = r_{22} \begin{pmatrix} a & b \\ c & 1 \end{pmatrix}. \tag{7}$$

 $\mathbf{T}_{Li}$  (i = 1, 2) is the WCM of a non reflective line having a length  $L_i$ ,  $\mathbf{T}_L$  is the WCM of a non reflective line having a length  $L_1/2$ ,  $\mathbf{T}_{DUT}$  is the WCM of the device under test and  $\Delta S = S_{11}S_{22} - S_{12}S_{21}$ .

## 2.1 Computation of $S_{21}$ and $S_{12}$ Using the Wave Propagation Vector $\lambda$

(Reynoso-Hernández J.A, Estrada-Maldonado C. F, 2000)

Using (1)-(3) and knowing that the determinant of product matrices is equal to the product of the matrix determinants, the following equations are derived (Wan CH, et al 1998)

$$\frac{\det(T_3)}{\det(T_1)} = \frac{S_{12}}{S_{21}},$$
(8)

$$\frac{\det(T_1 + T_3)}{\det(T_1)} = \det(T_{L_1} + T_L T_{DUT} T_L) , \qquad (9)$$

$$\frac{\det(T_2 + T_3)}{\det(T_1)} = \det(T_{L_2} + T_L T_{DUT} T_L).$$
(10)

Using (4)-(6) and (8), equation (9) and (10) are expressed in matrix form by

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ \frac{1}{\lambda} & -\lambda \end{bmatrix} \begin{bmatrix} 1/S_{21} \\ \Delta S/S_{21} \end{bmatrix},$$
(11)

where

$$p = \frac{\det(T_1 + T_3) - \det(T_3)}{\det(T_1)} - 1,$$

$$q = \frac{\det(T_2 + T_3) - \det(T_3)}{\det(T_1)} - 1,$$

and  $\lambda = e^{\gamma(L_2 - L_1)}$  (11bis).

Solving (11) for  $S_{21}$  and (8) for  $S_{12}$ , we have

$$S_{21} = \frac{1 - \lambda^2}{\lambda(q - \lambda p)},\tag{12}$$

$$S_{12} = \frac{\det(T_3)}{\det(T_1)} \frac{1 - \lambda^2}{\lambda(q - \lambda p)} .$$
(13)

It should be noted that when  $\lambda^2 = 1$ , (12) and (13) remain undetermined quantities. This occurs when angle  $(\lambda) = k \cdot 180^\circ$ , k = 0, 1, 2, ..., n and line losses are zero  $(\text{Ln}(\text{abs}(\lambda)) \neq 0$  since  $\text{abs}(\lambda) = 1$ ). However, due to line losses,  $\text{abs}(\lambda) \neq 1$ , and uncertainties in the computation of  $S_{21}$  and  $S_{12}$  are reduced at some specific frequencies for which angle $(\lambda) = k \cdot 180^\circ$ , k = 0, 1, 2, ..., n. As an example of this problem we plot in Fig. 2. the numerator and denominator of  $S_{21}$ . Notice from this-plot that both numerator and denominator of  $S_{21}$  exhibit a set of three minimums (close to zero but always above to zero) corresponding at electrical length of  $\pi$ ,  $2\pi$  and  $3\pi$ . Furthermore, as frequency increases, these minimums increases. This behavior could be attributed to the line losses.



Fig. 2 Plot of numerator and denominator of  $S_{21}$  given by Eq. 12 versus frequency

# 2.1.1 Computation of the Travelling Wave Vector $\lambda$

(Reynoso-Hernández, J.A, Estrada-Maldonado C.F, 2000)

The travelling wave  $\lambda$  is derived from (1), (2), (4), and (7) using the next procedure.

$$\mathbf{T}_{\mathbf{X}} = \mathbf{T}_{\mathbf{A}}^{-1} \mathbf{T} \mathbf{T}_{\mathbf{A}} , \qquad (14)$$

$$\mathbf{T}_{\mathbf{X}} = \mathbf{T}_{\mathbf{L2}} \quad \mathbf{T}_{\mathbf{L1}}^{-1} = \begin{pmatrix} \frac{1}{\lambda} & 0\\ 0 & \lambda \end{pmatrix}; \lambda \in C , \qquad (15)$$

$$\mathbf{T} = \mathbf{T}_{2} \ \mathbf{T}_{1}^{-1} = \begin{pmatrix} t_{11} & t_{12} \\ t_{21} & t_{22} \end{pmatrix}; t_{ij} \in C , \qquad (16)$$

Using (14)-(16), equation (14) becomes

$$\begin{pmatrix} \frac{1}{a} & 0\\ 0 & \lambda \end{pmatrix} = \frac{1}{a-bc} \begin{pmatrix} a(t_{11} + \frac{c}{a} t_{12} - bt_{21} - b\frac{c}{a} t_{22}) & bt_{11} + t_{12} - b^2 t_{21} - bt_{22} \\ a^2(-\frac{c}{a} t_{11} - (\frac{c}{a})^2 t_{12} + t_{21} + \frac{c}{a} t_{22}) & a(-b\frac{c}{a} t_{11} - \frac{c}{a} t_{12} + bt_{21} + t_{22}) \end{pmatrix}$$

$$(17)$$

Comparing each term of matrices on both sides of (17),  $\lambda$  is computed as a function of b and a/c by

$$\lambda = \frac{t_{22} + bt_{21} - \frac{b}{a/c}t_{11} - \frac{1}{a/c}t_{12}}{1 - \frac{b}{a/c}} = \frac{1 - \frac{b}{a/c}}{t_{11} + \frac{1}{a/c}t_{12} - bt_{21} - \frac{b}{a/c}t_{22}}$$
(18)

where

$$b^{2}t_{21} + b(t_{22} - t_{11}) - t_{12} = 0, \qquad (19)$$

$$\left(\frac{a}{c}\right)^2 t_{21} + \frac{a}{c}(t_{22} - t_{11}) - t_{12} = 0.$$
 (20)

It should be noticed that quadratic equations (19) and (20) have already been reported by (Engen and Hoer, 1979) but their derivation is different in this work. On the other hand, because of equal coefficients observed on (19) and (20), b and a/c are roots of the same equation. Moreover, since  $T_A^{-1}$  exists  $(a - bc \neq 0)$ , then b is different from a/cand hence b and a/c are the two different roots of (19) and (20). Values of b and a/c are chosen in accordance to the criterion reported on (Engen and Hoer, 1979).

## 3 Straightforward Determination of $S_{21}$ and $S_{12}$

Using (1) and (3), the following equations are derived

$$T_{DUT} T_{L1}^{-1} = T_A^{-1} T_3 T_1^{-1} T_A$$
 (21)

Now defining

$$\mathbf{T}_{3} \ \mathbf{T}_{1}^{-1} = \begin{pmatrix} p_{11} & p_{12} \\ \\ p_{21} & p_{22} \end{pmatrix}, \qquad (22)$$
$$\mathbf{T}_{DUT} \ \mathbf{T}_{L1}^{-1} = \frac{1}{S_{21}} \begin{pmatrix} -\Delta S & S_{11}e^{-\gamma L_{1}} \\ \\ -S_{22}e^{\gamma L_{1}} & 1 \end{pmatrix}. (23)$$

On the other hand, from (21) it should be notice that,  $T_{DUT} T_{L1}^{-1}$ , and  $T_3 T_1^{-1}$  are similar matrices and as a result they have the same *determinant*,  $(\Delta p = p_{11} p_{22} - p_{12} p_{21})$  that is,

$$\Delta p = \frac{S_{12}}{S_{21}} . \tag{24}$$

To separate  $S_{21}$  or  $S_{12}$  from (24) we need an additional expression. This expression is derived by putting (7) and (22) in (21) and expressed as

 $\mathbf{T}_{\mathbf{A}}^{-1}\mathbf{T}_{\mathbf{3}}\mathbf{T}_{\mathbf{1}}^{-1}\mathbf{T}_{\mathbf{A}} = \frac{1}{a-bc} \begin{pmatrix} a(p_{11} + \frac{c}{a}p_{12} - bp_{21} - b\frac{c}{a}p_{22}) & bp_{11} + p_{12} - b^2p_{21} - bp_{22} \\ a^2(-\frac{c}{a}p_{11} - \frac{c}{a})^2p_{12} + p_{21} + \frac{c}{a}p_{22}) & a(-b\frac{c}{a}p_{11} - \frac{c}{a}p_{12} + bp_{21} + p_{22}) \end{pmatrix}$ (25)

 $S_{21}$  is derived putting (23) and (25) in (21) and comparing each term of matrices on both sides. Finally  $S_{21}$ and  $S_{12}$  are expressed as

$$S_{21} = \frac{1 - \frac{b}{a/c}}{p_{22} + bp_{21} - \frac{1}{a/c}p_{12} - b\frac{1}{a/c}p_{11}}, (26)$$
$$S_{12} = \Delta p S_{21}.$$
(27)

It should be noted that for computing  $S_{21}$  and  $S_{12}$  using (26) and (27) we need the a/c and b values. As it can see, this procedure for deriving  $S_{21}$  and  $S_{12}$  indicates that the line parameters  $\gamma$  and  $\lambda$  are not needed. In other words, this procedure only needs the partial knowledge of the transition  $T_A$  alone. Regarding the a/c and b values, they can be determined using. (19) and (20) or using Eq.1 and a broadband 50 Ohms load, that is, the "long line" is replaced by a broad band load as in the Line reflect Match calibration technique (Eul H.J, et al, 1988).

# 3.1 Computation of *a/c* and *b* Using a L-M (Line - Broad Band Match) Method

An alternative way for determining b and a/c terms is using a nonreflecting line, Eq.1, and a broadband 50 Ohms load. From Eq.1 and solving for matrix T<sub>B</sub>, we have

$$\mathbf{\Gamma}_{\mathbf{B}} = [\mathbf{T}_{\mathbf{A}} \mathbf{T}_{\mathbf{L}\mathbf{I}}]^{-1} \mathbf{T}_{\mathbf{I}}$$
(28)

Defining T<sub>1</sub> as (Marks R.B, 1991)

$$T_1 = g \begin{pmatrix} d & e \\ & \\ f & 1 \end{pmatrix}.$$
 (29)

Using Eq.4 and Eq.5 the matrix  $T_B$  given by (28) becomes

$$T_{B} = \rho_{22} \begin{pmatrix} \alpha & \beta \\ & \\ \varphi & 1 \end{pmatrix}, \tag{30}$$

where

$$P_{22} = \frac{\frac{(1-\frac{c}{a}e)}{a}g}{(1-\frac{c}{a}b)}\frac{g}{r_{22}}e^{-2\gamma l_1},$$
(31)

$$\alpha = \frac{(d-bf)}{a\left(1-\frac{c}{a}e\right)}e^{2\gamma L_1},$$
(32)

$$\beta = \frac{(e-b)}{a(1-\frac{c}{a}e)}e^{2\gamma l_1},$$
(33)

$$\varphi = \frac{\left(f - \frac{c}{a}d\right)}{\left(1 - \frac{c}{a}e\right)},\tag{34}$$

It should be noted from Eq.34 that c/a can be easily determined if  $\varphi$  is known since *f*, *d* and *e* are elements of

 $T_1$  matrix and all of them are known. Then solving for c/a from Eq.34, we have

$$\frac{c}{a} = \frac{(\varphi \ e - 1)}{(\varphi - f)}, \qquad (35)$$

$$W_{1} \underbrace{\int_{k_{1}}^{q} S_{21}^{A} S_{22}^{A}}_{k_{1}} \underbrace{\int_{k_{2}}^{B} S_{21}^{A} S_{22}^{A}}_{\Gamma = 0} \xrightarrow{F = 0} \underbrace{\int_{k_{2}}^{q} S_{21}^{B} S_{22}^{B}}_{k_{2}} W_{2}$$

Fig. 3 Error model for transition  $T_A$  and  $T_B$  used for computing b and a/c

On the other hand, modeling the transition  $T_A$  and  $T_B$  as shown in Fig.3, b and  $\varphi$  values can be easily determined using a broad-band load (50 Ohms). The reflection coefficient  $W_1$  and  $W_2$ , measured as a function of reflection coefficient  $\Gamma_L$  are given as

$$W_{1} = S_{11}^{A} + \frac{S_{12}^{A} S_{21}^{A} \Gamma_{L}}{1 - S_{22}^{A} \Gamma_{L}} = \frac{a \Gamma_{L} + b}{c \Gamma_{L} + 1} , \qquad (36)$$

$$W_{2} = S_{22}^{B} + \frac{S_{12}^{B} S_{21}^{B} \Gamma_{L}}{1 - S_{11}^{B} \Gamma_{L}} = \frac{\alpha \Gamma_{L} - \varphi}{1 - \beta \Gamma_{L}}.$$
 (37)

Assuming that the refletion coefficient  $\Gamma_L$  of the broadband load is equal to zero (perfectly matched), the *b* and  $\varphi$ values are expressed as

$$W_1 = b,$$
$$W_2 = -\varphi.$$

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Notice that  $b = S_{11}^m$  and  $\varphi = S_{22}^m$ ;  $S_{11}^m y S_{22}^m$  are the scattering parameters measured when transitions are loaded with a broadband match. Once  $\varphi$  is computed the a/c term is determined using Eq.35.

The main advantage in the determination of b and a/c terms using a broadband load is that the difficulty in to discern b and a/c is eliminated. Furthermore, the condition that lines have to be lossy can be lifted.

#### **4 Results**

In order to show the usefulness of the proposed L-L and L-M methods, measurements were performed on PHEMTs (NE24200 with  $W_g = 200 \ \mu\text{m}$  and  $L_g = 0.25 \ \mu\text{m}$ ) and RFIC amplifiers (SGA5386 and SGA5389).

Prior to scattering parameters measurements, a two-tier calibration was performed on a HP8510C network analyzer in the frequency range of 0.045-50 GHz. The first tier calibration is performed with the SOLT calibration technique using a coaxial calibration kit from HP. With this calibration, the systematic errors of the network analyzer are achieved. The second tier calibration is performed using the L-L, L-M and the multilines LRL (Marks R.B, 1991) calibration techniques implemented using coplanarmicrostrip structures from a calibration kit ProbePoint<sup>™</sup> CMO5. The  $S_{21}$  and  $S_{12}$  parameters of a PHEMT transistor de-embedded with the multiline method were used as verification elements of calibrations. The transistor was mounted in a coplanar test fixture formed with two 50 ohms microstrip transitions supplied bv to coplanar JCmicrotechnology . Details of this test fixture are indicated in Fig. 1. Regarding the  $\lambda$  computation, Fig. 4 shows the broadband variations in the complex plane versus frequency of  $\lambda$  and  $1/\lambda$  computed from (18). It should be noticed a monotonous phase variation in the whole frequency band. Two spirals are observed resulting in monotonous phase variations: the first one turning contra clockwise represents a positive traveling wave and the second one turning clockwise represents a negative traveling. The spirals radius of  $\lambda$  and  $1/\lambda$  vary as:





0

 $Re(\lambda)$ 

0.5

-0.5

-1.5

-1

1.5

1

162



Fig. 5 Real and imaginary parts of  $S_{21}$  parameters versus frequency for the PHEMT NEC24200 measured at  $V_{DS}$ =2V

The frequency dependence of the two spiral radius indicates that the wave vanishes as frequency increases as expected in a lossy transmission line. Once  $\lambda$  or  $1/\lambda$  is determined,  $S_{21}$  and  $S_{12}$  versus frequency is computed for each of the investigated devices.



Fig. 6 Real and imaginary parts of  $S_{12}$  parameters versus frequency for the PHEMT NEC24200 measured at  $V_{DX}=2V$  and  $V_{GX}=0$ Vmeasured with L-L and LRL(m)



Fig. 7 Layout of the calibrations standards used for RFIC SGA-5386 and RFIC SGA-5389

Transmission scattering parameters  $S_{21}$  and  $S_{12}$  of a PHEMT (*NEC242000* biased at  $V_{DS} = 2$  V and  $V_{GS} = 0$  V) calculated with the *L-L* method of this work (equations (12)-(13) and (26)-(27)) and computed with the multilines (Marks R.B, 1991) *LRL* calibration technique are reported in Fig. 5. and Fig. 6. Concerning the measurement of the small signal gain of the RFIC SGA5386 and SGA5389 amplifiers, we utilize a test fixture fabricated with substrate FR4. Details of this test fixture are shown in Fig.7. Measurements of the small signal gain of these RFIC amplifiers with *L-L* and multilines *LRL* calibration techniques are reported in Fig. 8-9.



Fig. 8 Small signal gain versus frequency for the RFIC SGA-5386 measured at V=3.2V and I=24mA



Fig. 9 Small signal gain versus frequency for the RFIC SGA-5389 measured at V=3.1V and I=18mA

It should be noticed from Fig. 5-6 and Fig. 8-9 that there are a good agreement between the  $S_{21}$  and  $S_{12}$  parameters for the PHEMT, and the small signal gain for the RFIC amplifiers, computed with L-L and with multiline methods. These results validate the accuracy of the L-L method proposed in this work.

On the other hand, plots of  $S_{12}$  and  $S_{21}$  computed using the L-M procedure (b and a/c determined with a broadband load) and L-L method are shown in Fig. 10-11. We observe from these plots some "spikes" in the trace of real and imaginary of  $S_{12}$  and  $S_{21}$  when they are computed with the L-L procedure. By contrast, when  $S_{12}$  and  $S_{21}$  are determined with the L-M procedure a free spike traces are

observed. The "spikes" problem arises because the term  $\left|1 - \frac{b}{a/c}\right|$  is undetermined at some frequencies and this happens when the electrical length of  $L_2$ - $L_1$  is equal to  $k \cdot 180^\circ$ , k = 0, 1, 2, ..., n. To illustrate this result in Fig. 12 we plot  $\left|1 - \frac{b}{a/c}\right|$  versus frequency for b and a/c determined with a 50 Ohms load and two lines.



Fig. 10 Real and imaginary parts of  $S_{21}$  parameters versus frequency for the PHEMT NEC24200 measured at  $V_{DS}$ =2V and  $V_{GS}$ =0Vmeasured with *L*-*L* and L-M methods



Fig. 11 Real and imaginary parts of  $S_{12}$  parameters versus frequency for the PHEMT NEC24200 measured at  $V_{DS}=2V$  and  $V_{GS}=0V$ measured with *L-L* and L-M methods



measured with two lines or with a match

### **5** Conclusions

In this paper, a new broadband de-embedding method was proposed to efficiently evaluate the  $S_{21}$  and  $S_{12}$  parameters of two-port (active or passive) using two non reflecting lines (L-L) and a line and a matched load (L-M). The main advantage of the proposed method is that nor the physical lengths nor the wave propagation constant of the lines used in the de-embedding are needed. The important variables are the *b* and a/c ratios and the travelling wave vector  $\lambda$ , which is calculated by a novel matrix approach using two non reflecting lines (L-L) or a non reflecting line and a matched load (L-M). The  $\lambda$  expression in terms of *b* and a/c ratios allows  $\lambda$ , and hence  $S_{21}$  and  $S_{12}$ , to be computed in broadband. This method can be used for a fast evaluation of the transducer power gain  $G_T$  and the maximum stable gain  $G_{ma}$  of transistors and amplifiers.

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J. Apolinar Reynoso-Hernández, he received the Electronics and Telecommunications Engineering degree, M. Sc. degree in Solid State Physics and Ph. D. degree in Electronics, from ESIME-IPN, Mexico, CINVESTAV-IPN, Mexico and Université Paul Sabatier-LAAS du CNRS, Toulouse, France, in 1980, 1985 and 1989 respectively. Since 1990 he has been a researcher at the Electronics and Telecommunications Department of CICESE in Ensenada, B. C., Mexico. His research activities are concerned with physical device modeling, accurate microwave and millimeter wave measurements techniques for active device characterization and model parameter extraction. Dr. Reynoso-Hernández is member of editorial board of the IEEE Transaction on Microwave Theory and Techniques.